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**Electrical Characterization of
Traditional and Aerosol Jet
Printed Conductors under
Tensile Strain**

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Motivation

Address current hurdles within flexible and stretchable electronics development:

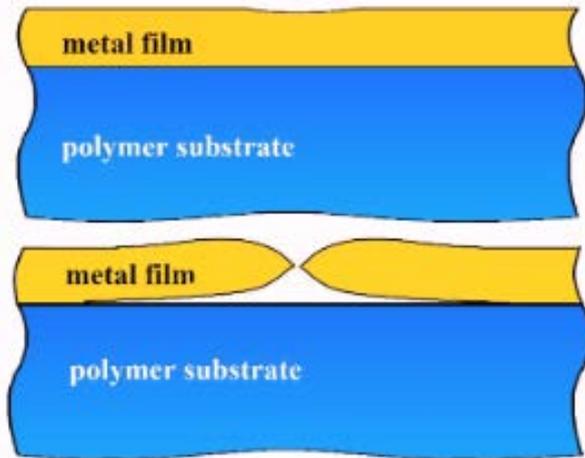
- ✧ *How to overcome mechanical mismatch between conductor and dielectric?*
- ✧ *What happens to electronics and interconnects under strain?*
- ✧ *Which materials and fabrication methods best tolerate strain?*



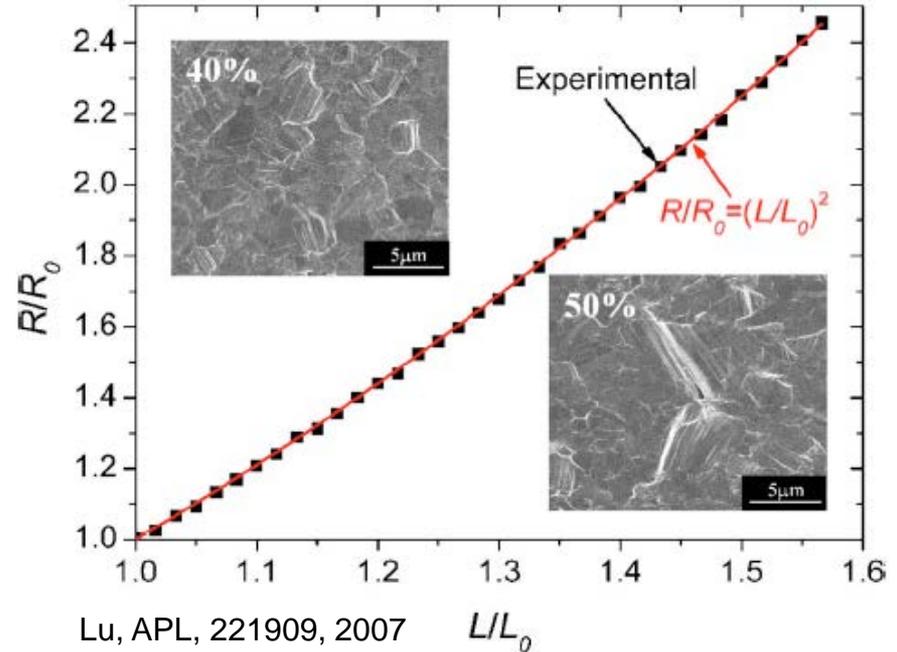
Chihaya Adachi & Hajime Nakanotani Lab

Prior Research: Metals Under Tensile Strain

Xiang, APL,
161910, 2005



Metals under strain { **Strong adhesion (top)**
Weak adhesion (bot)



All resistance increase due to geometric change; no measurable discontinuities initiated in film

Strong adhesion at interface in data shown

Resistance in Conductors Under Strain

$$R = \underline{R_C} + \underline{R_D} = \underline{R_0(1 + \varepsilon)^2} + \left[\frac{\rho L(1 + \varepsilon)}{A} \right] m^{\frac{1}{\alpha(1 + \varepsilon)}}$$

Continuous Resistance Increase
(material independent)

Lu, APL, 221909, 2007

Discontinuous
Resistance Increase
(material dependent)

Cairns, et al., APL, 76, 2000

- ✧ **Discontinuities include cracks, buckles, losses of adhesion, etc.**
- ✧ **For ideal conductor, $R_D \rightarrow 0$, $R = R_C$**
- ✧ **Novel addition to previous work:**
 $\alpha =$ discontinuity-percolation factor
- ✧ **α quantifies tendency of discontinuities to propagate and unify at higher strain**

R_0 = initial resistance
 ε = engineering strain
 ρ = resistivity of underlying conductor
 L = characteristic discontinuity length
 A = characteristic discontinuity area
 m = number of discontinuities
 α = discontinuity-percolation factor

Resistance in Conductors Under Strain

$$R = \underline{R_C} + \underline{R_D} = \underline{R_0(1 + \varepsilon)^2} + \left[\frac{\rho L(1 + \varepsilon)}{A} \right] m^{\frac{1}{\alpha(1+\varepsilon)}}$$

Continuous Resistance Increase
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Discontinuous
Resistance Increase
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$$m(R, \varepsilon) = \left\{ \left[\frac{R}{R_0} - (1 + \varepsilon)^2 \right] \frac{R_0 A}{\rho L(1 + \varepsilon)} \right\}^{\alpha(1 + \varepsilon)}$$

- ✧ Determine α from m at known R , ε
- ✧ Describe microscale phenomenon
- ✧ Preference is for α to be close to 1
(no discontinuity percolation)

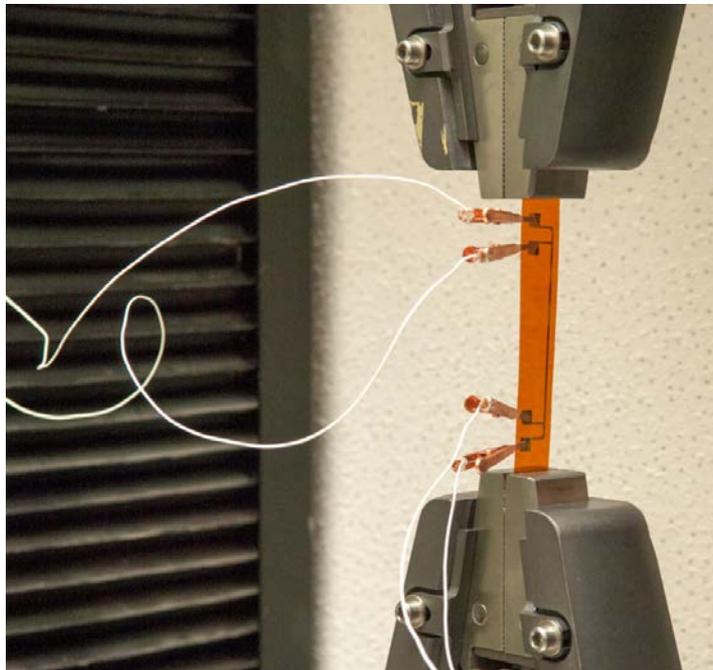
R_0 = initial resistance
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Methods and Materials: Sample Preparation

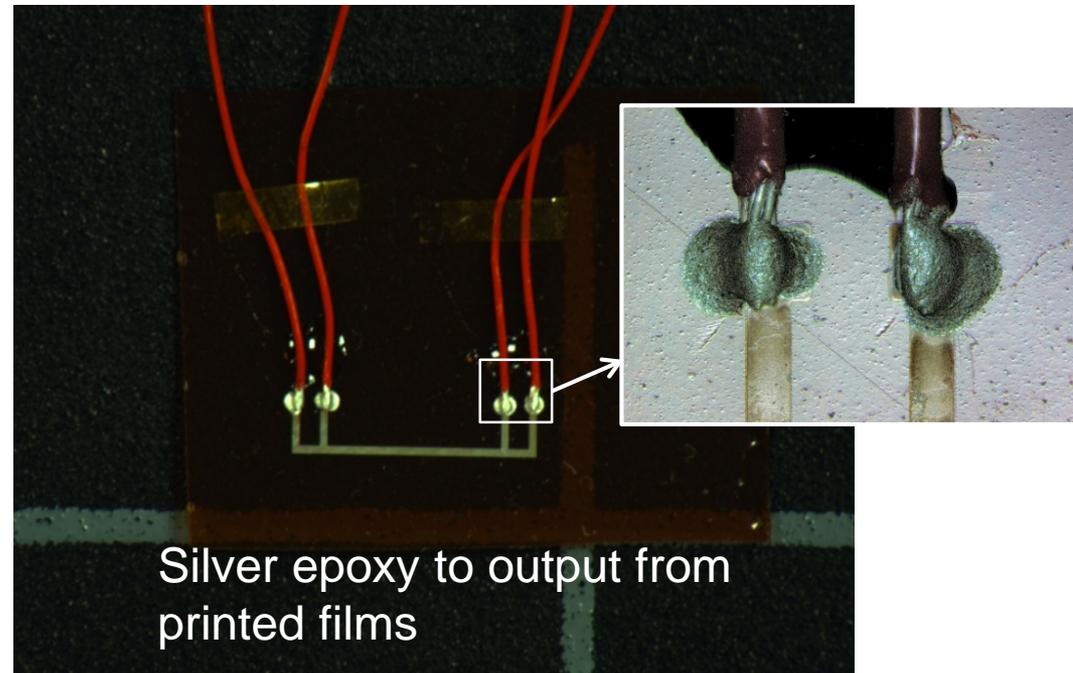
- ✧ Substrates: PDMS, Kapton
- ✧ Conductors: Silver (evaporated), Gold (evaporated), Silver ink (printed)
- ✧ Evaporated samples deposited to 100nm target thickness (100-110nm actual thickness) in TEMESCAL electron beam evaporator at $P = 2-3 \times 10^{-7}$ Torr
- ✧ Printed samples deposited in Optomec aerosol jet printer (2 μ m thickness) and laser sintered

Methods and Materials: Strain Conditions and Data Acquisition

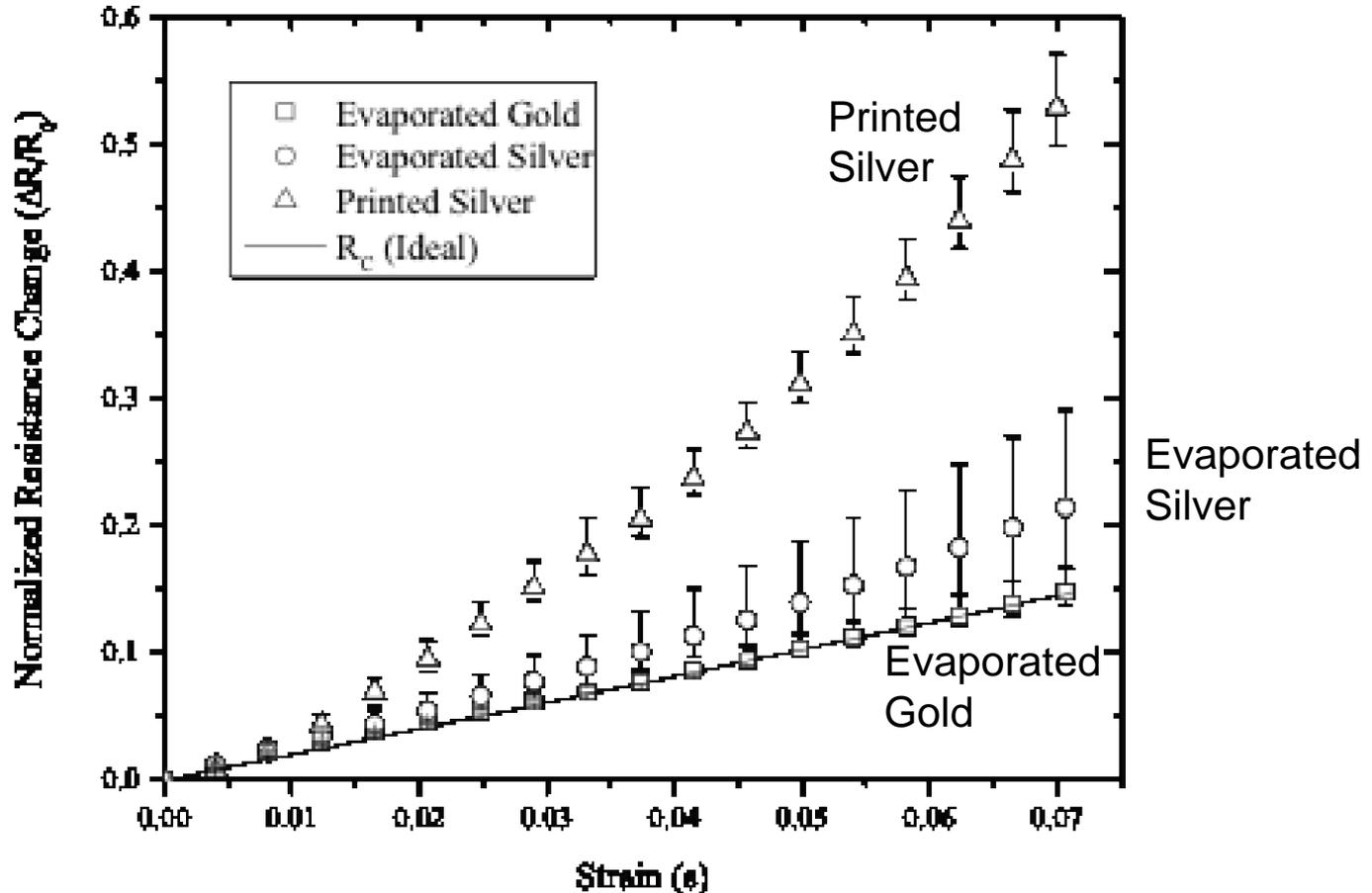
- ✧ Resistance monitored using 4-wire measurements while stretching in Instron tensile tester at rate of 10% strain/minute



Alligator clips to output from evaporated films

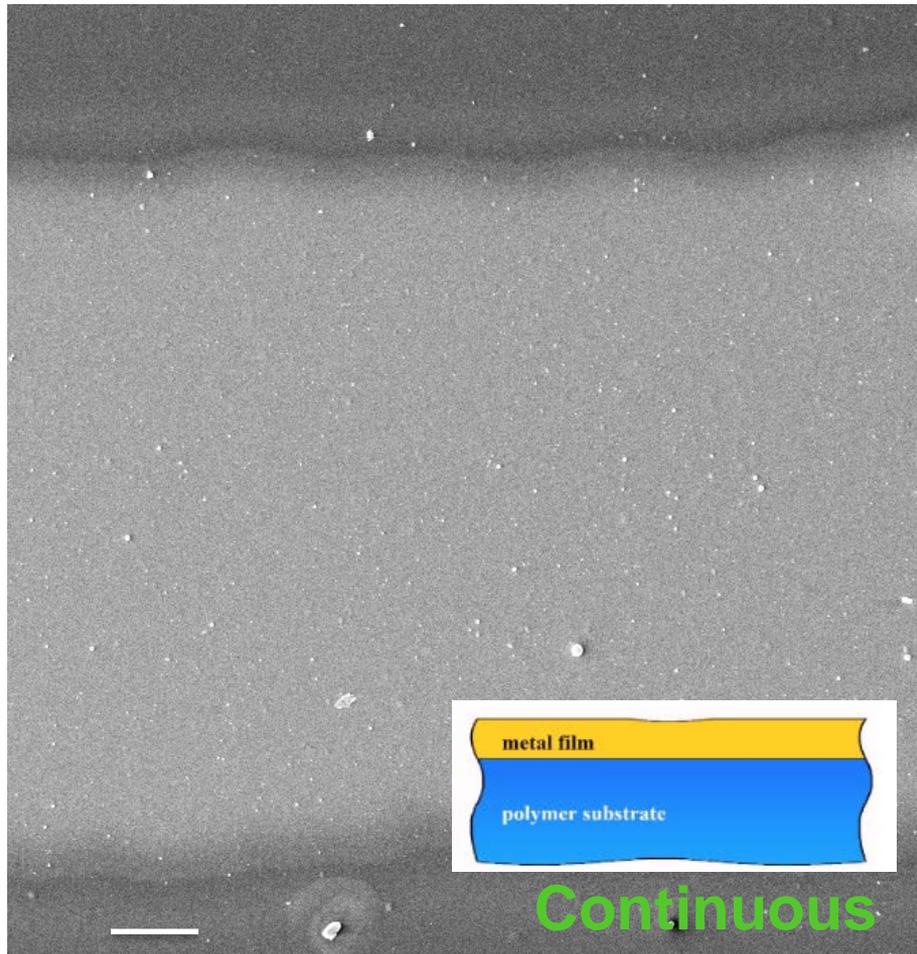


Conductor-Kapton Systems Under Strain

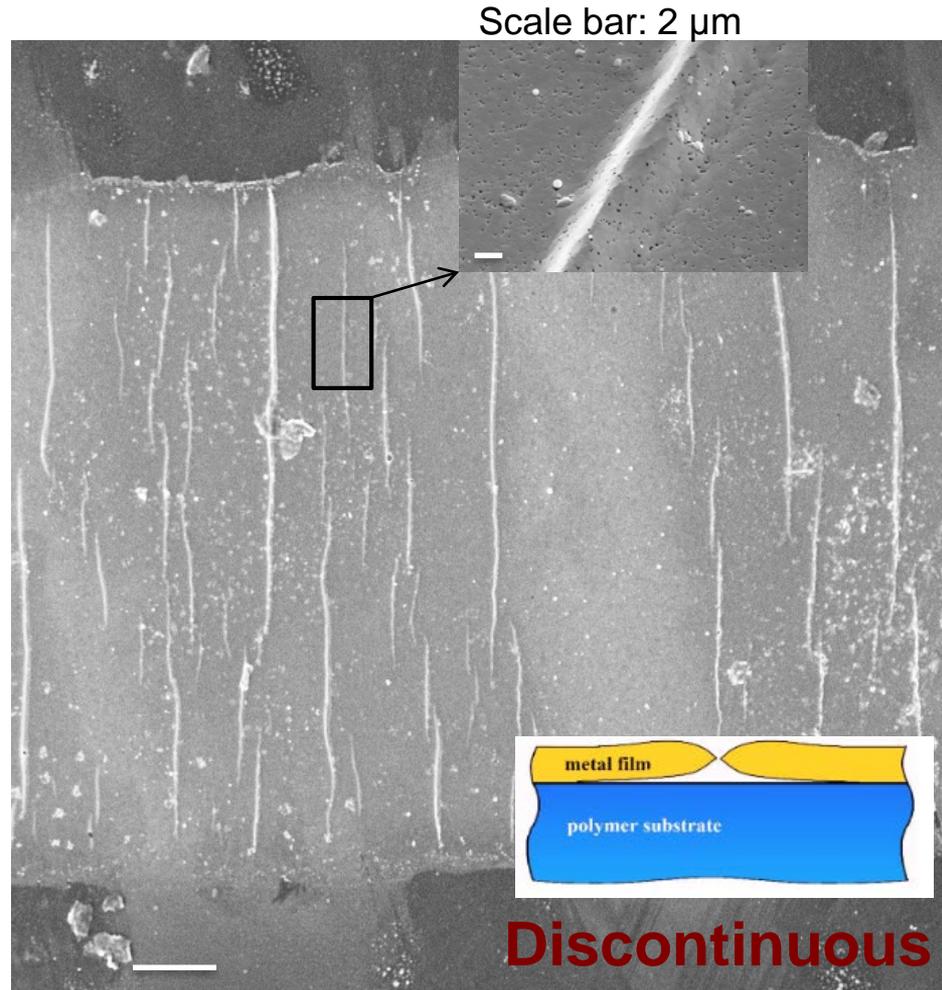


- ✧ Only continuous resistance increase in gold sample
- ✧ Evaporated silver superior to printed silver

Evaporated Silver-Kapton After Strain



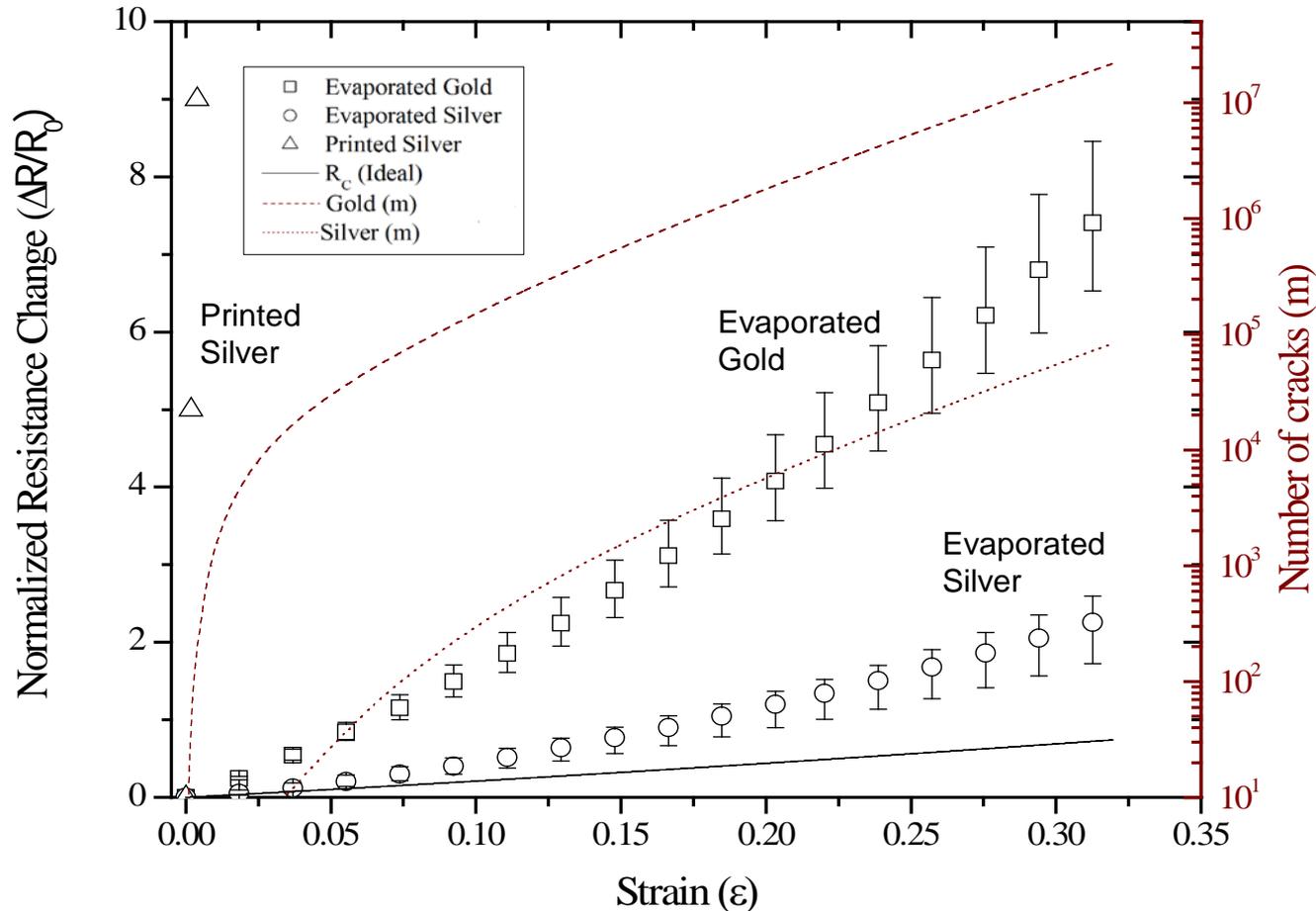
Scale bar: 100 μm



Scale bar: 100 μm

- ✧ $1.1 < \alpha < 2.1$; exact value not attainable, crack depth unknown
- ✧ In discontinuous section, adhesion loss led to buckling

Conductor-PDMS Systems Under Strain



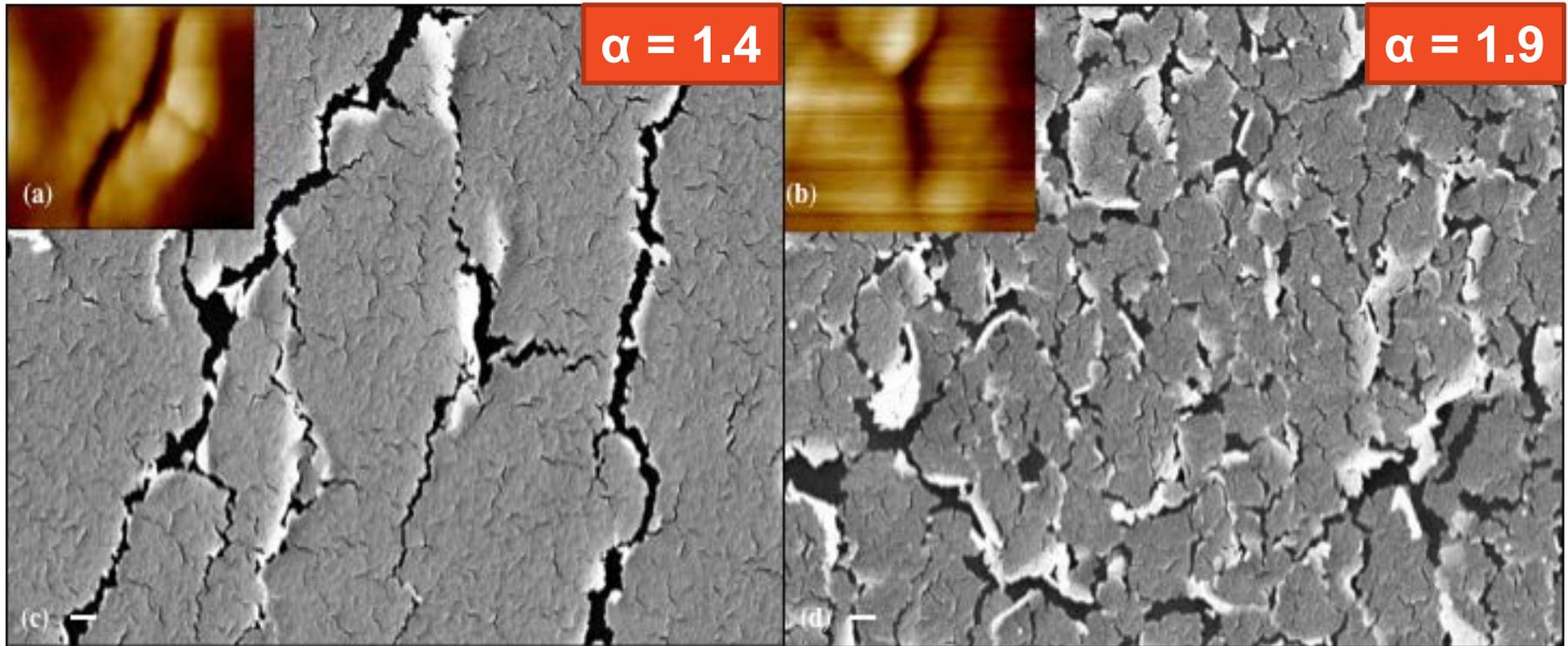
- ✧ Significant discontinuity induced resistance across all materials
- ✧ Printed silver completely inelastic
- ✧ Evaporated silver “best”

$$m(R, \epsilon) = \left\{ \left[\frac{R}{R_0} - (1 + \epsilon)^2 \right] \frac{R_0 A}{\rho L (1 + \epsilon)} \right\}^{\alpha(1 + \epsilon)}$$

Conductor-PDMS Systems Under Strain

Gold (100nm) on PDMS

Silver (100nm) on PDMS



Scale bar: 2 μm

Scale bar: 2 μm

- ✧ AFM (a,b) \rightarrow discontinuity depth; SEM (c,d) \rightarrow discontinuity length, width
- ✧ Qualitative inspection supports quantitative α determination

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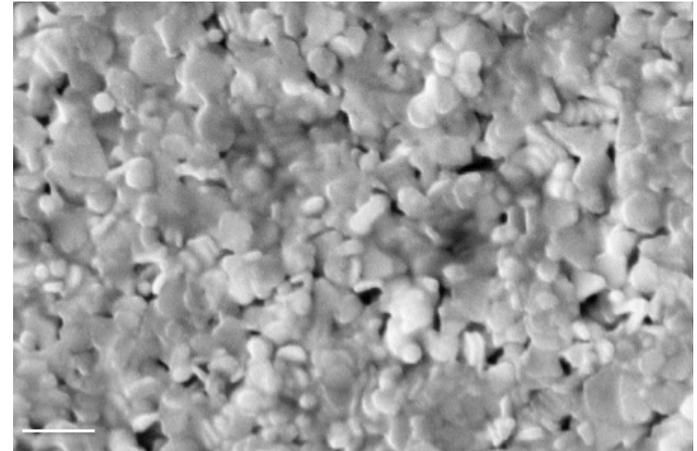
$$m(R, \varepsilon) = \left\{ \left[\frac{R}{R_0} - (1 + \varepsilon)^2 \right] \frac{R_0 A}{\rho L (1 + \varepsilon)} \right\}^{\alpha(1 + \varepsilon)}$$

Printed Silver

✧ After inspecting post-strained printed silver samples, there were **no discernible discontinuities**

✧ **Initial resistivity 10x bulk silver resistivity**

✧ Current additive manufacturing techniques have intrinsic discontinuities



Scale bar: 1 μm

✧ **Applying tensile strain intensifies discontinuities;** lower modulus polymer does as well

✧ Applying small strain and returning polymer to initial length restores resistance to R_0

Conclusions

- ✧ Evaporated metals are likely more tolerant to tensile strain than any additively manufactured conductor
- ✧ Developed model to describe conductor resistance during strain
- ✧ Validated model via experimental and qualitative analysis as way to describe microscopic phenomenon with easily attainable data
- ✧ Achieved through α – material dependent “discontinuity percolation factor” (e.g. propagation of cracks, delamination, buckles, etc.)

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Conductor-Polymer Systems Under Tensile Strain

- ✧ Unstretched state: $R_0 = \frac{\rho L_0}{A_0}$
 - ✧ Stretched state: $R = \frac{\rho L}{A}$
 - ✧ Assuming volume maintained: $AL = A_0 L_0$
- $\frac{R}{R_0} = \left(\frac{L}{L_0}\right)^2 = (1 + \varepsilon)^2 = R_C$
- ✧ R_C is the ideal case; resistance increase **only** caused by changing geometry, **no** material failure

R_D: Discontinuity Induced Resistance

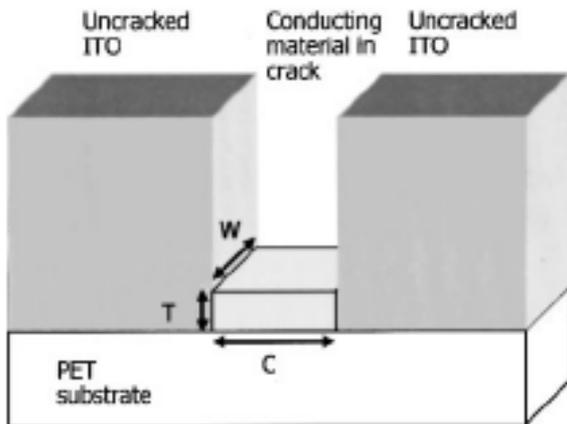
ITO under tensile strain

$$R_D = \frac{\rho \lambda^2}{V} \sum_{i=1}^m (\varepsilon - \varepsilon_{ci})^2$$



Conductor-polymer systems under tensile strain

$$R_D = \left[\frac{\rho L(1 + \varepsilon)}{A} \right] m^{\frac{1}{\alpha(1+\varepsilon)}}$$



Problems:

1. All ITO discontinuities were cracks that traversed the width of the film
2. Rapid loss of electrical continuity

Solutions:

1. More adaptable
2. α = “discontinuity-percolation factor”

R_D = discontinuity induced resistance
 m = number of discontinuities
 ρ = resistivity of underlying conductor
 λ = length scale of discontinuity
 ε = strain
 ε_{ci} = strain at initiation of discontinuity
 V = volume of underlying conductor
 L = characteristic discontinuity length
 A = characteristic discontinuity area
 α = discontinuity-percolation factor

Cairns, et al., APL, 76, 2000